Self-Referential Probability

I study languages that can express:

(π) The probability of π is not greater than or equal to 1/2.

Connection to the liar paradox:

 (λ) λ is not true

Seemingly harmless principles like introspection now lead to contradictions.

Why consider such sentences? §1.1.1

These arise in languages that can express:

- Georgie is (probabilistically) certain that Dan believes to degree 1/2 that the coin will land heads.
- Every sentence has probability greater than or equal to 0.

Can give us options for how to deal with cases like promotion:

Alice will get a promotion just if she does not have a degree of belief greater than or equal to 1/2 that she'll get it.

Developing a semantics Part I

Use possible world structures to provide the facts about probability. E.g.



Allows for varying extensions of P.

• The obvious definition

 $w\models_{\mathfrak{M}}\mathsf{P}_{\geqslant r}\ulcorner\varphi\urcorner\iff m_w\{v\mid v\models_{\mathfrak{M}}\varphi\}\geqslant r,$

is often not satisfiable. (ch. 2)

Useful technique: Generalise semantics given for the liar paradox.

- Kripkean semantics Non-classical probabilities.
 - Strong Kleene (ch. 3) Also obtain an axiomatisation.
 - Supervaluational (ch. 4) Provides imprecise probabilities.
- Revision theory (ch. 5) Classical probabilities, but non-terminating sequence of models.

Rationality Requirements Part II

The accuracy argument (ch. 7) and the Dutch book argument (ch. 8). I formalise and study proposals by Caie:

Consider how good a credal state would be were the agent to adopt it (i.e. if it were the interpretation of P).

- Leads to unwieldy rationality constraints (§7.2)
 - Non-probabilistic,
 - Non-introspective,
 - Negative,
 - Non-logically-omniscient.

We should instead:

Evaluate a credal state from the initial credal state's perspective.

Different formulations of this allow for the different semantics as developed in part I.